## Lesson 20. Absolute Minima and Maxima

- $(a, b)$ is an absolute minimum if $f(a, b) \leq f(x, y)$ for all $(x, y)$ in the domain of $f$
- $(a, b)$ is an absolute maximum if $f(a, b) \geq f(x, y)$ for all $(x, y)$ in the domain of $f$
- Every absolute minimum is a local minimum
- However, a local minimum is not necessarily an absolute minimum!

- Same statements apply for absolute maxima and local maxima

Example 1. Find the shortest distance from the point $(2,0,-3)$ to the plane $x+y+z=1$.

Example 2. Find three positive numbers whose sum is 90 and whose product is a maximum.

Example 3. A rectangular box is to be made from $100 \mathrm{~m}^{2}$ of cardboard. Find the maximum volume of such a box.

